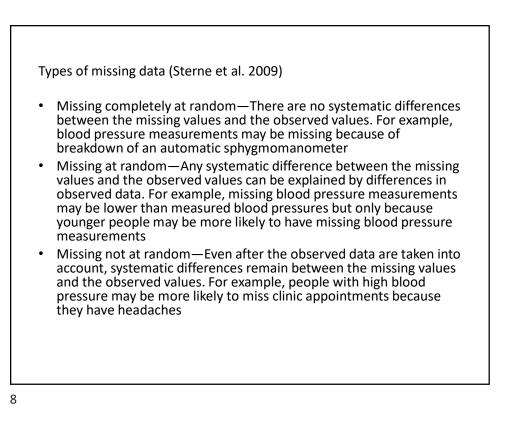


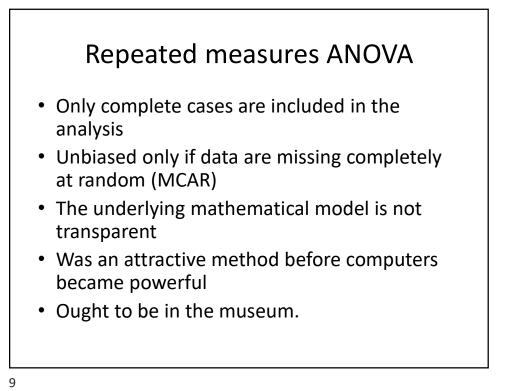
| Types of missing data | The probability that a data |
|------------------------------|-----------------------------|
| (Missing data mechanism) | value is missing |
| | (unobserved) can depend on |
| MCAR | Neither observed or |
| Missing Completely at Random | unobserved values |
| (Mangler helt tilfeldig) | |
| MAR | Only observed values |
| Missing at Random | |
| (Mangler betinget tilfeldig) | |
| MNAR | Unobserved values (and |
| Missing Not at Random | observed values) |
| (mangler ikke-tilfeldig) | , í |

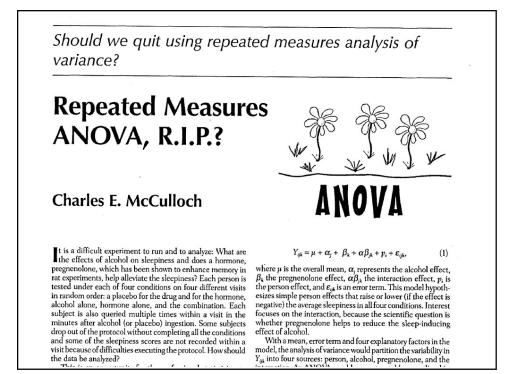
Lydersen, S. 2019. Manglende data - sjelden helt tilfeldig. Tidsskrift for Den norske legeforening, 219, (3) 269

Lydersen, S. 2019. Manglende uttrykk for manglende data. Tidsskrift for Den norske legeforening, 219, (3) 278

| Engelsk term | Norsk term | Beskrivelse |
|-------------------------------------|-------------------------------|---|
| Missing completely at random (MCAR) | Mangler helt tilfeldig | Sannsynligheten for manglende data avhenger verken av observerte eller uobserverte data |
| Missing at random (MAR) | Mangler betinget tilfeldig | Sannsynligheten for manglende data avhenger bare av observerte data |
| Missing not at random (MNAR) | Mangler ikke- tilfeldig | Sannsynligheten for manglende data avhenger av uobserverte data |

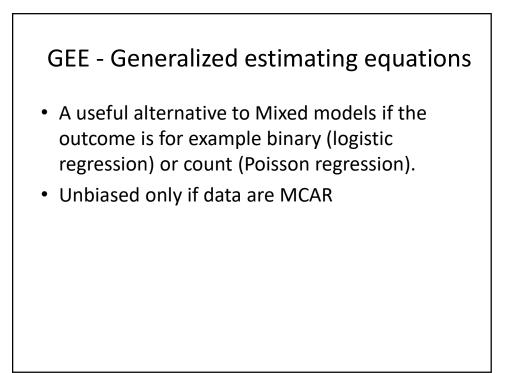


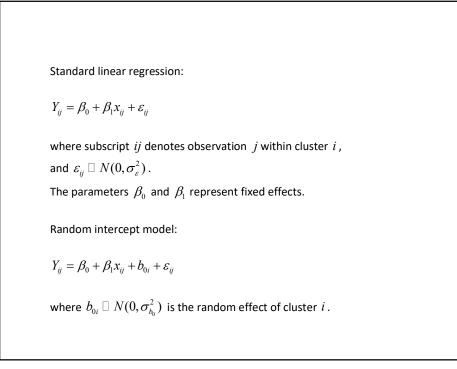


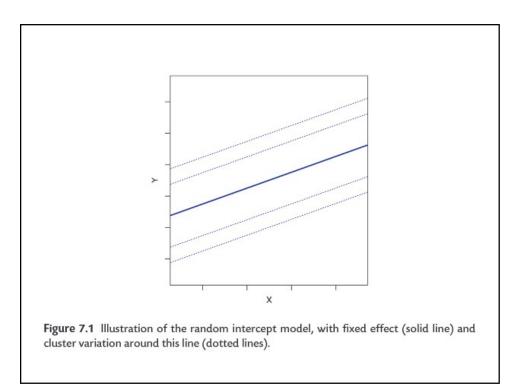


Mixed models

- Includes all subjects, also those with missing data at some time point(s)
- Unbiased under the less restrictive missing at random (MAR) assumption (for linear models)
- Transparent mathematical model







Random intercept and random slope:

$$Y_{ij} = \beta_0 + \beta_1 x_{ij} + b_{0i} + b_{1i} x_{ij} + \varepsilon_{ij}$$

where $b_{\mathrm{l}i} \square N(0, \sigma_{b_{\mathrm{l}}}^2)$ represents the random slope for cluster i .

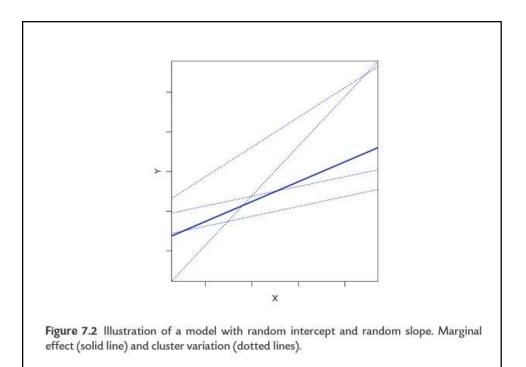
Note 1:

In (almost) every statistics package, the default is to assume the random effects b_{0i} , b_{1i} (...) to be independent. This is completely unrealistic: Generally, their covariances are nonzero. So their variance-covariance matrix must be specified as unstructured.

Note 2:

Adding one or more random slopes causes a large increase in the number of parameters, and make estimation computationally very demanding or impossible.





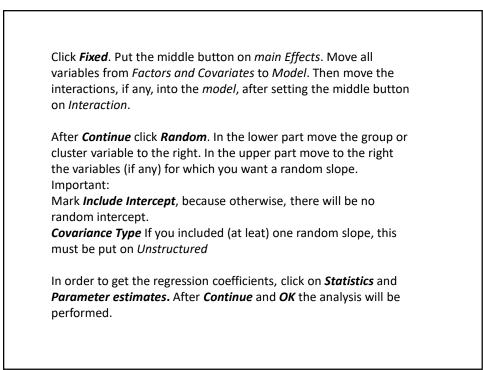
Multilevel analysis in SPSS (with two levels)

The data file must be in "long" format, that is, one line per observation within the cluster. You can convert the file from "wide" to "long" format using **Data**, **Restructure**, and *restructure selected variables into cases*.

Choose Analyze, Mixed Models and Linear.

Move the group or cluster variable to Subjects. Continue.

Add the outcome variable in *Dependent Variable*. Continuous covariates go into *Covariate(s)*, and categorical covariates go into *Factor(s)*. Dichotomous covariates may alternatively go into *Covariate(s)*.



References

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